Universal Banking, Asymmetric Information and the
Stock Market

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ABSTRACT

The paper shows that attempts to sell stocks of borrowing firms by the universal banks upon private information result in: (i) discounting of stock prices, (ii) a higher fraction of ownership in the borrowing firm and a greater loan size, (iii) an increase in consumption risk and precautionary savings of households. Hence, the size of the commercial banking activity increases under asymmetric information at the expense of a higher consumption risk borne by the households. The magnitude of the resulting stock market discount depends crucially on the market’s perception about the relative proportion of lemons in the stock market. The stock market discount and the resulting consumption volatility can be considerably reduced by a credible punishment scheme implemented by the government the form of fines. However, it imposes a deadweight loss on private citizens. On the other hand, ring fencing of retail banking could entail significant loss of national welfare because of the restrictions imposed on bankers’ diversification opportunities.

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I. Introduction

A universal bank can sell insurance, hold equity in non-financial firms and underwrite securities in addition to performing its commercial banking operations. In recent times, functioning of all such activities under the umbrella of a single financial institution has been a subject of a heated debate. The regulators in the UK and the USA are contemplating to curb multifarious activities of these institutions, especially in areas where commercial banks enter the business of underwriting equities.\(^1\) The current discussion partly mirrors the similar debate that took place in mid 90’s prior to the repeal of Glass-Steagall Act.\(^2\) During the aftermath of financial crisis, the debate now focuses on whether integrated system imposes greater risks on households and much of the basis for such concern lies in too much private information held by a unified financial system.

However, it is also of utmost importance to know the mechanism and the consequences of the universal banking system where much of the private information was generated due to bank’s involvement in multiple branches of financial activities. In this context, our paper demonstrates that the institution of universal banking works best in the absence of any information friction. The hallmark of the system is that it provides full risk sharing and consumption smoothing arrangements for bank’s clients in a world without asymmetric information. However, when the banker/underwriter possesses private information about the potential success or failure of the projects that they had funded and in addition, holds claims in tradable securities in them, it destroys both consumption insurance and smoothness properties. Such a possibility may distinctively emerge in scenarios when some banks, hit by bad shocks, can sell their ownership claims to public on the pretext of meeting their liquidity crunch and the investors cannot distinguish whether such sale is triggered by bad information or due to banks’ liquidity considerations. Our paper shows that breaking down of perfect risk sharing arrangements due to conflicts of interests stemming from private information also leads to (a) a sharp discount in the price of stocks underwritten by banks (b) greater self insurance of agents leading to a higher volume of deposits

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\(^1\)The Financial Times (21th December, 2012) reported "In a 146-page assessment of the government’s planned Vickers reforms, the 10-member panel endorses the central idea that “universal” banks should be made to erect a protective “ringfence” around their high-street banking activities........ The report also raises the prospect of a ban on proprietary trading – whereby banks trade securities for their own account – in line with the incoming Volcker rule in the US.” In an earlier report (April 21st, 2011), the newspaper also discussed about "global convergence" of the policy makers views regarding separation of various segments of activities that fall under the purview of Universal Banking.

and (c) loan pushing by the banks.

The novelty of our paper is that we investigate the impact of such a conflict of interest not only on the pricing of securities but also on the commercial banking activities of the universal banks which comprise (a) the volume of lending and (b) the magnitude of depository activities. In addition, we also analyze the real output effect of such conflict of interest. Thus our analysis ultimately traces the combined effects of such conflict of interest on both risk sharing and consumption smoothing of households as well as on the aggregate output.

The building block of the paper’s framework is the traditional model of banking in which financial intermediaries transform riskier loans made to individuals to relatively safer deposits by holding a diversified portfolio of loans to many projects with uncorrelated risks. See, for example, Azariadis (1993, page 238-244), Bhattacharya and Thakor (1993) and Diamond (1984) and Gurley and Shaw (1960) for exposition of this view. We deliberately follow this approach to grasp the additional mileage of the Universal banking over standard framework of intermediation, which focuses on economies of scale or scope associated with such banking system.\(^3\) Hence, we integrate a conventional model of banking with optimal financial contracts between bank and its borrowers. Embedding the optimal financial contracts in a traditional model of banking generates a structure of a financial institution that resembles universal banking where banks hold both deposits and tradable financial securities of their client firms.

In our model, a lemon problem emerges when banks can sell these financial claims in a secondary market due to either considerations towards meeting an exogenous liquidity shock or because of negative private information about the economy. This introduces a nontrivial signal extraction problem for investors who can not decipher the real cause of sale of such securities and encounter the risk of buying a lemon security. The demand for such speculative stock purchase comes from the households who form an optimal portfolio of safe bank deposits and risky shares based on risk-return trade-off where the source of risk stems from the purchase of a lemon securities.\(^4\)

\(^3\)Our paper also differentiates from the extant literature on the Universal Banking which brings in either certification effects or economies of scope or transmission of information to outsiders. For example, see Kanatas and Qi (1998, 2003) for the trade-off between economies of scope embedded within Universal banking versus deteriorations of quality of projects and innovations, Puri (1996, 1999) for the added role of certification of banks while underwriting debt securities versus conflicts of interests in equity holding, and Rajan (2002) for efficiency of universal banking related to competitiveness of the institutions.

\(^4\)Our paper is thus closer in spirit to the recent analysis of conflict of interest in other areas of financial services industry rooted in the informational problems. See Mehran and Stultz (2007) (and other papers in the volume) for a comprehensive analysis of such conflicts pertinent to financial services industry originating from asymmetry of information.
Our simple model provides insights about the effect of information friction in the universal banking system on household’s risk bearing activities and its consequent effect on the stock market and the aggregate economy. First, as rational investors assign a probability that banks might be selling lemons, such securities sell at a discount. The model simulation suggests that this discount is quantitatively substantial and it depends on the probability of a sale of lemon imputed by investors. Second, the immediate effect of this sale due to information friction disrupts the perfect risk sharing arrangements obtained under full information. This happens because losses incurred by the investors from buying a probable lemon security even with a discount are not fully compensated at the margin when securities turn out to be good. The unevenness in investor’s income manifests in the increased volatility in consumption across states of nature which entails welfare loss of households. Third, to mitigate this consumption risk, households undertake more savings resulting in an increased volume of bank deposits. Fourth, banks make extra profit from selling lemon stocks which is channelled (via their balance sheet) towards greater loan pushing to households. Finally, the effect of holding and trading financial claims upon information spills over to both investment and commercial banking activities which might cause a decline in the aggregate investment and output because of a higher market interest rate.

The US experiences during the wake of the financial crisis and its aftermath are in line with the prediction of our model. Commercial banking activities showed a spurt after 2004. During 2004Q1-2008Q4, the quarterly savings deposit:GDP ratio rose from 20.6% to 30% while the quarterly commercial and industrial loans also showed an increase from about 7.6% of GDP in 2004 to 11.3% until the onset of the credit crunch. This increase in commercial banking activity was accompanied by a sharp drop in the quarterly GDP growth rate from 1.5% to -0.2% and about a 30% decline in the real S&P index.5

Although our paper does not aim to provide an explanation of the financial crisis, it provides useful insights about the risk taking role of the universal banks. An implication of our model is that the universal banking system could have possibly contributed to the crisis only to the extent that bankers had hidden information about the borrowing firms. This might have led to the lemon problem in the stock market. How much information was actually hidden in the banking system is an empirical question which is beyond the scope of this paper. The policy

5 These data are reported from the quarterly database of the Federal Reserve Bank of St Louis. The S&P index is deflated by the CPI (all items) to arrive at the real stock price index comparable to our model.
implication of our model is that a universal banking system could work efficiently if there is full disclosure of negative information. A punitive tax on banks could moderate the lemon problem in the stock market due to information friction and lower the consumption risk of the households. However, such a tax entails some efficiency loss because the enforcement authority suffers from the same information friction as private citizens and thus imposes this tax on all banks regardless of their deviant status.

We address the issue whether private agents are better off if a legal mandate prohibits retail banks to underwrite securities as per the independent banking commission’s recommendation. Using our model we demonstrate that such a "ring fencing" could lead to a substantial welfare loss compared to universal banking arrangement because risk diversification opportunities are shut down by such legislation.\(^6\)

The paper is organized as follows. The following section lays out the model and the environment. Section 3 solves a baseline model of universal banking with full information about the states of nature. Section 4 introduces the asymmetric information about the states and the consequent conflict of interest between banks and the stockholders. Section 5 performs two policy experiments based on our model, namely (i) the effects of imposing punitive fines on banks to prevent bank misbehaviour, (ii) effects of banning banks’ underwriting securities. Section 6 concludes.

II. The Model

A. Households

We consider a simple intertemporal general equilibrium model in which there is a continuum of identical agents in the unit interval who live only for two periods. At \( t = 1 \), a stand-in agent is endowed with \( y \) units of consumption goods, and she also owns a project requiring a physical investment of \( k \) units of capital in the current period which produces a random cash flow/output in the next period. The production of output is subject to two types of binary shocks: (i) an aggregate shock, (ii) an idiosyncratic shock. The aggregate shock is transmitted to intermediaries/agents via a probabilistic signal. A signal conveys news about the state which could be high (\( h \)) and low (\( l \)) with probabilities \( \sigma_h \) and \( 1 - \sigma_h \) respectively. A low signal (a

\(^6\)To the best of our knowledge, the only recent paper which analyzes the macroeconomic effects of retail and universal banking and makes welfare comparison is Damjanovic, Damjanovic and Nolan (2012) in a DSGE framework. However, they do not address the effect of lender’s moral hazard on the stock market premium which is the central aim of our paper.
recessionary state) triggers widespread liquidation of the current projects and the project is liquidated at a near zero continuation value ($m$).\(^7\) If the signal is $h$, agents are still subject to idiosyncratic shock which manifests in terms of a project success which means that output is $\theta_s g(k)$ with probability $p$ and failure meaning output equal to $\theta_b g(k)$ with probability $1 - p$ where $\theta_s > \theta_b$.\(^8\)

To sum up, the random output in next period has the following representation:

\[
\begin{align*}
m & \text{ with probability } 1 - \sigma_h \\
\theta_s g(k) & \text{ with probability } \sigma_h p \\
\theta_b g(k) & \text{ with probability } \sigma_h (1 - p)
\end{align*}
\]

B. Banks

At date 1, competitive universal banks offer an \textit{ex ante} contract that stipulates (a) deposits ($s$), (b) loans ($f$), and (c) contingent payments ($d_i$, $i = g, b$). After writing such a contract and before the realization of the random shock, banks may experience a liquidity shock ($C$) which necessitates banks to sell their ownerships claims ($\theta_i g(k) - d_i$) to the public in a secondary market at a price $q$.\(^9\) Let $N$ be the number of such securities. Let $x$ and $nx$ denote the states of liquidity shock and no such shock with probabilities $\gamma$ and $1 - \gamma$. This interim period when the secondary market opens is dated as 1.5.\(^10\)

At this interim date 1.5, the bank may also acquire an early signal about the aggregate shock. If the signal is high ($h$) with probability $\sigma_h$, the project’s value upon continuation is greater than the same under liquidation. If the signal is low, it means that banks get early information

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\(^7\)This assumption is made in order to preserve a simple structure for analysis. Instead of assuming a fixed salvage value, we could have alternatively proceeded with a lower probability of success in individual projects in the event of a low aggregative signal and this would not change our results.

\(^8\)Since this type of risk is distributed independently across infinite number of projects, the law of large number holds in an economy populated by continuum of agents so that $p$ fraction of individuals is more successful than the rest. On the other hand, no such law holds for a low aggregate state.

\(^9\)We only allow the banks to have a liquidity shock and exclude individuals to have similar problem because it makes the exposition simpler and also owing to the fact that the primary purpose of the paper is to investigate the consequence of banks’ holding of tradable financial assets on the rest of the economy under both full information and asymmetric information. In particular, we show later how the private information gathered by banks regarding the aggregate state has both financial and real effects. In this scenario, allowing individuals to incur liquidity problems will add further noise in the financial market and will actually strengthen our results.

\(^10\)Under universal banking, banks or intermediaries can hold securities which are otherwise unrestricted and tradable compared with the system where banks can only hold debt securities which cannot easily be traded in the financial/debt market.
that most of the projects will turn out to be a lemon with a negligible value \( m \) (close to zero).\(^{11}\)

At \( t = 2 \), uncertainties get resolved and all agents receive pay-off according to the contracts written at date \( t = 1 \), which, in turn, depends on (a) resolution of individual uncertainty and (b) occurrences of liquidity shocks of banks. The Figure 1 summarizes the timeline in terms of a flow chart assuming that households and banks have symmetric information about the timing of shocks.

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\[^{11}\text{The rationale behind such assumption is that since banks lend and monitor a large number of projects across the economy, they gather expertise to collect information relevant not only to a single project but can extract information about the overall economy better than the households. This is a standard function of banks who are also known as “informed lenders” (see Freixas and Rochet, 2008). However, the main difference between the universal and non universal banking is that the former can take its informational advantage by selling stocks to others before the bad event realizes while the latter cannot do such things because they are not allowed to hold equity in the borrowing firms.}\]
rationale for households to hold claims in the form of bank deposits (i.e., demand deposits in addition to holding financial claims via optimal contracts). Household’s saving also provides liquidity to the stock market when it opens at the intermediate date 1.5. Saving thus performs two roles: (i) consumption smoothing, (ii) liquidity for speculative purchase of shares.

The expected profit of the bank is thus:

\[
\pi^{bank} = \sigma_h \gamma \cdot [p \{ \theta_g g(k) - d_g \} + (1 - p) \{ \theta_b g(k) - d_b \}] \\
+ \sigma_h (1 - \gamma) \cdot (qN - C) \\
+ (1 - \sigma_h) m - f \cdot (1 + r \sigma_h) 
\]

We just note that the loan servicing cost is \(r \sigma_h\) because banks do not pay any interest on savings in a low signal state which occurs with probability \(1 - \sigma_h\). Hereafter, we assume that banks issue just enough shares to cover the liquidity crunch which means \(N = C/q\).\(^{12}\)

C. Preferences

The utility function of each household/ borrower/depositor is additively separable in consumption at each date and is of the form:

\[
U = u(c_1) + v(c_2) 
\]

where \(c_t = \) consumption at date \(t\), where \(t = 1, 2\), \(u(\cdot)\) and \(v(\cdot)\) are: (a) three times continuously differentiable, (b) concave, and (c) have a convex marginal utility function. Hence, agents are risk-averse and in addition, they have a precautionary motive for savings.

Apart from the current period, in period 2 there are 5 possible states and the expected utility of an agent from consumption that occur in all such contingencies is given by:

\[
EU = [u(c_1) + \sigma_h \gamma \{pv(c_{2g}^{nx}) + (1 - p)v(c_{2b}^{nx})\}] \\
+ \sigma_h (1 - \gamma) \{pv(c_{2g}^x) + (1 - p)v(c_{2b}^x)\} \\
+ (1 - \sigma_h) u(c_2) 
\]

\(^{12}\)In fact, when information friction is present (which we deal in the later section), it is not incentive compatible for any bank to issue more shares such that \(qN > c\). If a bank does so, it will be labelled as a deviant bank by the investors.
The superscripts $x$ and $nx$ stand for liquidity or no liquidity shock for banks\footnote{Although individuals do not suffer any liquidity shock, banks’ state of liquidity matter to them because it determines the state whether they will participate in the stock market or not.} and the subscript $2g$ and $2b$ stand for good and bad project outcomes (idiosyncratic shocks) at date 2 with the good news about aggregate shock (subscript $h$) and the subscript $l$ refers to the low aggregate state. The other notations are as follows:

- $c_1 = \text{consumption of the agent in the first period.}$
- $c_{2j}^{nx} = \text{consumption of the agent in the period 2 when the banks with high aggregate signal do not suffer liquidity shock (nx) and the individual state is } j = g \text{ or } b, \text{ which means that the cash flow is } \theta_{jg}(k).$
- In a similar vein, $c_{2j}^x = \text{consumption of the agent in the period 2 when the banks with a high signal suffer liquidity shock (x) and the individual state is } j.$
- $c_{2l} = \text{consumption of the agent when the bank has received a low signal and face liquidation of the project.}$

The first term, $u(c_1)$ in (3) is the utility from current consumption. The term $\sigma_h \gamma \{pv(c_{2g}^{nx}) + (1 - p)v(c_{2b}^{nx})\}$ is the probability weighted utility when the aggregate news is good but banks do not suffer liquidity shock. Similarly, the term $\sigma_h (1 - \gamma) \{pv(c_{2g}^x) + (1 - p)v(c_{2b}^x)\}$ is the probability weighted utility in a good aggregate state when banks suffer liquidity shock. The final term $(1 - \sigma_h)u(c_{2l})$, is the weighted utility in the bad aggregate state when banks do not pay interest to depositors.
D. Budget Constraints

The budget constraint in period 1 and all five contingencies in period 2 are:

\[
c_1 = y + f - s - k \tag{4}
\]
\[
c_{g2}^{nx} = d_g + s(1 + r) \tag{5}
\]
\[
c_{b2}^{nx} = d_b + s(1 + r) \tag{6}
\]
\[
c_{g2}^{x} = d_g + (s - z)(1 + r) + \frac{z}{q} \left( \bar{\theta} g(K) - \bar{d} \right) \tag{7}
\]
\[
c_{b2}^{x} = d_b + (s - z)(1 + r) + \frac{z}{q} \left( \bar{\theta} g(K) - \bar{d} \right) \tag{8}
\]
\[
c_{l2} = s - z \tag{9}
\]

where \( \bar{\theta} = p\theta_g + (1 - p)\theta_b, \bar{d} = pd_g + (1 - p)d_b \) and \( K \) is the average capital stock in the economy.

The equation (4) is the first period budget constraint which states that consumption of an agent is equal to endowment \( y \) plus the fund received from bank \( f \) less the money stored as deposit \( s \) and expenditure on capital good \( k \). The equations (5) and (6) capture agents’ consumption (equal to income) in the good and bad states of production respectively when banks do not suffer any liquidity shocks. In these states of nature, individuals do not participate in the stock market in the intermediate period. In such states, the agent’s income consists of two parts: (i) the contingent payments \( d_i \) depending on the state of production, \( i = g, b \), (ii) the principal and the interest income on deposits \( s(1 + r) \).

Equations (7) and (8) are the state dependent budget constraints when banks encounter liquidity shock and the project can be a success \( (g) \) or failure \( (b) \). When the household member invests \( z \) in stocks at a unit price \( q \), it entitles him a claim of \( \frac{z}{q} \left( \bar{\theta} g(K) - \bar{d} \right) \) units of goods because the bank sells a mutual fund to the household bundling good and bad shares. An atomistic bank while stipulating an optimal contract for an atomistic household takes the average variables, \( K \) and \( \bar{d} \) as given. However, in equilibrium these two average variables are determined by aggregate consistency conditions.

Equation (9) shows that when the bank receives a bad news \( (state \ l) \) about the economy, the project is liquidated and the banks receive the liquidation value as it has the first priority over claims. Recall that in such a low signal state (which is a state of macroeconomic shock),

\[\text{A bank lends out to infinitely many people. Hence, an individual over a unit interval, when buys one such bank’s mutual fund receives a payment of } \{p\theta_g + (1 - p)\theta_b\}g(K) - \bar{d} \text{ per share.} \]
banks are unable to make full payment and only return the deposits $s$ to the households.\(^\text{15}\)

### III. Universal Banking under Full Information

As a baseline case, we first lay out the equilibrium contract in a full information scenario. For a given interest rate $r$ and stock price $q$, each bank offers a package to the household which includes (i) the loan size $f$, (ii) payments to the same household $d_i$ contingent on realizations of idiosyncratic states. In return, the household must put in a deposit $s$ at the same bank and undertake a physical investment $k$ in the project. Such a package is stipulated by the bank that solves the expected utility of the household subject to the condition that these universal banks offering such competitive contracts satisfy the participation constraint which means that they must break even.

The optimal contract facing the household is to maximize the expected utility (3) subject to the budget constraints given by (4) through (9) and zero profit constraint of the intermediary, i.e.

$$
\pi_{\text{bank}} = \sigma_h \gamma [p\theta_g g(k) - d_g] + (1 - p)(\theta_h g(k) - d_h)] + (1 - \sigma_h) m + \sigma_h (1 - \gamma) (qN - C) - f. (1 + r \sigma_h) \geq 0
$$

Since there is full information, the agent exactly knows the node at which the bank operates. Thus at a low signal state agents know that a stock market will not open at date 1.5. This immediately means that $z = 0$ at this low signal state.

### A. Interest rate

We assume here that the real interest rate, $r$ is fixed by a policy rule. Any discrepancy between borrowing $f$ and lending $s$ is financed by a net inflow of foreign funds (call it $NFI$) from abroad at this targeted interest rate.\(^\text{16}\) The appendix A provides the details of the market clearing conditions.

**Proposition 1:** The competitive equilibrium contract has the following properties:

(i) Contingent Payments: $d_g = d_b = d$ (say) such that $\frac{\gamma u'(c_1)}{1 + r \sigma_h} = v'(d + s(1 + r))$

(ii) Share Price: $q = \frac{E\tilde{X}}{1 + r}$ where $E\tilde{X} = \frac{\theta_g (K) - \tilde{d}}{N}$.

\(^{15}\)Nothing fundamentally changes in our model if we assume instead that banks return only a fraction of savings in a low aggregate state.

\(^{16}\)This assumption is made for analytical simplicity because it rules out the second order effect of the financial operations of banks and households on the real interest rate. In the next section where we undertake simulation, we allow the interest rate to vary to equilibrate the loan market.
(iii) Consumption: \[ c_{2g} = c_{2b} = c_{2b} = d + s(1 + r) = c_2 \text{ (say)} > c_2l = s \]

(iv) Saving: \[ u'(c_1) = \left[ \frac{(1-\sigma_h)(1+\sigma_h)}{1-\gamma \sigma_h + r \sigma_h (1-\gamma)} \right] \frac{u'(s)}{1 + r} \]

(v) Investment: \[ \sigma_h \gamma \bar{\theta} g'(k) = 1 + r \sigma_h \text{ where } \bar{\theta} = \bar{p} \theta_g + (1 - \bar{p}) \theta_b \text{ and} \]

(vi) Loan: \[ f = \sigma_h \gamma (\bar{\theta} g(k) - d) \frac{(1-\sigma_h)(1+\sigma_h)(1-\gamma)(qN-C)}{1 + r \sigma_h} \]

(vii) Consistency of Expectations: \[ k = K \]

**Proof:** Appendix B.

**Discussion:** (i), (iv), (v) and (vi) together determine \( \{d, s, K, f\} \) and the equation (ii) determines \( q \), given an exogenous \( r \). Stocks have fair market value as seen in (ii) and the risk premium is thus zero. The risk neutral bank bears the whole idiosyncratic risks which explains why the market risk premium is zero. (i) and (ii) together state that conditional on the realization of high signal, an agent receives a constant sum \( d \) across all states of nature. Although idiosyncratic risk is washed out in the high state \( h \), in the low state individuals are still exposed to negative aggregate shock which explains the last inequality of (iii). The holding of deposit in the form of savings acts as an instrument to deal with this situation. If there is no aggregate risk, \( \sigma_h = 1 \), optimal saving is zero as seen from (iv) which highlights the precautionary motive for savings. (v) states that the expected marginal productivity of investment equals the risk adjusted interest rate, \( 1 + \sigma_h r \). The physical investment \( k \) is lower if the probability of low aggregate state is higher (lower \( \sigma_h \)) or the probability of liquidity shock is higher (lower \( \gamma \)). In the latter case, banks may cut back lending and hold less equity stake due to looming insolvency\(^{17}\). (vi) states the equilibrium loan size obtained from bank’s zero profit condition. Finally, (vii) states the aggregate consistency condition that sum of all individual capital stocks equals the aggregate capital and over a unit interval.

The results in the proposition 1 serve to capture the basic functioning of the universal banking in the simplest possible full information framework. The universal banks optimally share project risks by offering a riskfree payment \( d \) and the residual \( \theta_j g(k) - d \) is kept by the bank.\(^{18}\) Without any conflicts of interest (asymmetric information), this is a Pareto optimal contract. It eliminates idiosyncratic uncertainties in household consumption and makes stock price trade at a fair market value.\(^{19}\)

\(^{17}\)In the simulation experiment reported in Table 3 later this conjecture is confirmed.

\(^{18}\)This contract is equivalent to: (i) agents holding a preferred stock (or any other instrument that ensures a constant sum in all contingencies within good aggregate state), and (ii) banks owning ordinary stocks and thus bear all the residual risks. Thus, banks holding of equity, a hallmark of universal banking, emerges as a mechanism of an optimum allocation of risk.

\(^{19}\)Although banks are holding the residual claim in each state but our conclusions are not sensitive to this
IV. Universal Banking under Asymmetric Information

Using the baseline model of full information described in the preceding section, we now turn to the case of asymmetric information. The basic tenet of such informational asymmetry is that banks hold private information about the realization of the aggregate business cycle as well the liquidity shocks.\textsuperscript{20} In other words, banks observe true realizations of both liquidity shocks and the realization of the signal regarding the macro business cycle state but agents know only the distribution of liquidity shocks and the signals. Since interest payment on deposits take place at $t = 2$ after the transaction in intermediate stock market, if the stock market opens at date $1.5$, agents cannot ascertain whether banks have received a low signal or simply suffered a liquidity shock. This gives rise to a typical lemon problem because universal banks with a low realization of the signal may sell off the equity held by them in the borrowing firm with a pretense of the liquidity shock. This problem of selling lemon stocks can emerge only in the universal banking system as opposed to the non universal system where banks are barred to hold equity in the borrowing firms.

\textsuperscript{20}The banks can observe the aggregate shock at least in a partial manner because they lend it to agents economy-wide and collect/collate information from each borrower. Hence, they tend to have economy-wide information while each agent is too small to acquire aggregate signal. However, bank’s signal about aggregate and idiosyncratic shocks need not be perfect and could be even noisy. For the sake of parsimony, simplicity, and without compromising our results below, we ignore the noisiness of bank’s signal about aggregate shock and their private information about individual projects.
Figure 2 summarizes the timeline of universal banking in the presence of asymmetric information. The only difference from Figure 1 is the dotted line at the node $t = 1.5$ which represents the fact that the agent cannot ascertain at this node whether the bank has suffered a liquidity shock or has received a low aggregate signal. At this node, she only observes whether the stock market has opened or not. If the stock market does not open then she knows for sure (a) high signal has occurred and (b) no bank has suffered a liquidity shock. Of course, she could still either succeed or fail. Given that (a) and (b) happen with probability $\gamma \sigma_h$, the expected utility (up to this node) is:

$$\sigma_h \gamma [pv(d_g + s(1 + r)) + (1 - p)v(d_b + s(1 + r))].$$

If the equity market opens at the intermediate date 1.5 where a financial intermediary sells stocks, an agent concludes that either the bank has received a low signal (with a probability of $1 - \sigma_h$) or the bank has received good news about the aggregate shock but it is still selling the stock because it has suffered a liquidity shock. The probability of the latter event is $\sigma_h (1 - \gamma)$. Hence, an individual at the node at date 1.5 when she is observing someone selling the stocks will impute the probability $\left( \frac{\sigma_h (1 - \gamma)}{\sigma_h (1 - \gamma) + (1 - \sigma_h)} = \frac{\sigma_h (1 - \gamma)}{(1 - \gamma) \sigma_h} \right)$ that the stock is not a lemon. The model
thus portrays a situation where banks lend money to its borrowers and also hold other tradable financial claims on them. Hence, our model is rich to capture a scenario whereby a bank can sell off lemon securities to investors when it has private information about bad project state underlying these securities, enabling it to recover some of its lending losses.

Define $EU_a$ as the expected utility in the presence of information friction. The optimal contract problem can be thus written as:

$$\max_{\{d_g, d_b, s, z, l, k\}} EU_a = \left[ u(y + f - s - k) + \sigma_h \gamma [pv(d_g + s(1 + r)) + (1 - p)v(d_b + s(1 + r))] \right. $$

$$+ (1 - \gamma \sigma_h) \cdot \left( \frac{(\sigma_h(1 - \gamma))}{(1 - \gamma \sigma_h)} \right) [pv(d_g + (s - z)(1 + r) + \frac{z}{q}E \bar{X}) $$

$$+ (1 - p)v(d_b + (s - z)(1 + r) + \frac{z}{q}E \bar{X}) \right] $$

$$+ (1 - \gamma \sigma_h) \left( \frac{1 - \sigma_h}{1 - \gamma \sigma_h} \right) v(s - z) $$

subject to

$$\pi^\text{bank}_a = \sigma_h \gamma [p\{\theta g(k) - d_g\} + (1 - p)\{\theta h g(k) - d_b\}] + \sigma_h (1 - \gamma)(qN - C) + (1 - \sigma_h)(qN + m) - f(1 + r \sigma_h) \geq 0 \quad \text{(10)}$$

There are two important features of this optimal contract problem which require clarification. First, while writing a contract with the bank, household/shareholder takes into account that banks can sell off stocks in the midway (at date 1.5) in the wake of bad news and thus they may incur capital losses. Second, the zero profit constraint (11) now contains an additional term $(1 - \sigma_h)qN$ which is the extra expected income of the banks from selling securities upon bad news.

**Proposition 2**: The equilibrium contract under asymmetric information has the following properties:

(i) Contingent Payments: $d_g = d_b = d_a$ (say) and $\gamma v'(c_{1a}) = \gamma v'(c_{2a}) + (1 - \gamma)v'(c_{2a})$

(ii) Share Price: $\frac{E \bar{X}_a}{q} - (1 + r) = \left( \frac{v'(s - z)}{v'(s_a - z) d_a + (s - z)(1 + r) + \frac{z}{q}E X} \right) \frac{1 - \sigma_h}{\sigma_h(1 - \gamma)} > 0$ where $E \bar{X}_a$

$$= \theta g(K) - d_a$$

(iii) Consumption: $c_{2g} = c_{2b} \equiv c_{2a}$ (say) $= d_a + s_a(1 + r) + \left\{ \frac{E \bar{X}_a}{q} - (1 + r) \right\} \cdot z > c^\text{pr}_{2g} = c^\text{pr}_{2b} \equiv c^\text{pr}_{2a} \quad \text{(say)}$

$$= d_a + s_a(1 + r) > c_{1a} = s_a - z$$

(iv) Saving: $u'(c_{1a}) = \left[ \frac{(1 - \sigma_h)(1 + r \sigma_h)}{1 - \gamma \sigma_h + r \sigma_h(1 - \gamma)} \right] v'(s - z)$
(va) Investment: \( \sigma_h \gamma \bar{g}'(k) = 1 + r \sigma_h \) where \( \bar{\theta} = p \theta_h + (1 - p) \theta_l \) and

(via) Loan: \( f_a = \frac{\sigma_h \gamma (\bar{g}(k) - d_a) + (1 - \sigma_h)qN + m + \sigma_h (1 - \gamma)(qN + C)}{1 + r \sigma_h} \)

(viia) Consistency of Expectations: \( k = K \)

**Proof:** Appendix B.

**Discussions:** We denote the subscript \( a \) as the solution of the variables under asymmetric information. (ia) shares the same feature as (i). Idiosyncratic risks are again borne by the risk neutral bank and household receives a riskfree payment \( d_a \) for its ownership claim to the project.

The major difference from the baseline full information setting appears in (iia). Since banks can potentially sell lemon securities in the midway at date 1.5, the optimal contract embeds this possibility. (iia) shows that stocks sell at a discount in the sense that the price is less than the discounted value of the cash flow. To put it alternatively, a positive market risk premium emerges in equilibrium to reflect this lemon problem.

The intuition for (iia) goes as follows. If a household spends one unit to buy stock from a bank, the marginal utility gain is:

\[
v' \left\{ d_a + (s - z)(1 + r) + \frac{z}{q} EX \right\} \left\{ \frac{EX}{q} - (1 + r) \right\}
\]

which happens with the probability, \( \sigma_h (1 - \gamma) \) that he buys stocks from a good bank suffering from a liquidity shock. On the other hand, the marginal cost is that if the purchased stock is a lemon, then he loses out on his savings and consequent marginal utility loss is \( v' \{(s - z)\} \) which happens with probability \( (1 - \sigma_h) \). The equivalence between the marginal gain and loss in investing in stocks explains that the stocks are selling at a discount (or equivalently the emergence of risk premium) as shown in the equation (iia). Everything else equal, the greater the ratio of \( \frac{1 - \sigma_h}{\sigma_h (1 - \gamma)} \) (relative proportion of lemon), the lower the price of the stock.

The immediate implication of stocks selling at a discount is captured in proposition (iiiia) which shows that the consumption flows of households are smoothed out only partially when banks sell their ownership claims upon bad news. The consumption in the states where households participate in the stock market exceeds the consumption in states where they do not. (iva) and (va) are the usual first order conditions for saving and investment. (via) shows the equilibrium loan size based on the zero profit constraint that binds at the optimum.\(^{21}\)

\(^{21}\)The description of overall equilibrium is omitted as they mirror conditions laid out in the appendix, except that the variables now refer to the asymmetric information case.
Comparison with the full information baseline reveals that the stock market risk premium arises purely due to information friction. Since shareholders are unable to ascertain whether banks sell off shares due to liquidity shock or arrival of bad news, additional premium is required to lure households to buy shares. The emergence of a risk premium (or stocks selling at a discount) prevents the agents from smoothing out consumption across \( nx \) and \( x \) states. In sharp contrast, a full insurance across \( nx \) and \( x \) is possible under full information setting because agents are perfectly informed about the nodes at which banks sell stocks.

The sale of stocks at a discount ex post, certainly changes the structure of contracts between banks and the borrowing households and it affects investment and commercial banking directly. The following proposition makes it evident.

**Proposition 3:** (i) \( d > d_a \); (ii) \( s < s_a \); (iii) \( f < f_a \).

**Proof:** Appendix C.

Since \( s < s_a \) and \( f < f_a \), the immediate implication is that the equilibrium loan size is higher under asymmetric information. From (iii) and (iiia), it follows that the spread between the expected consumption in the high and low aggregate signals under adverse selection is greater than under full information.

The intuitive reasonings of the above results are as follows. Since risk averse individuals undertake greater risks in the equity market than before due to possibilities of buying lemons, they are compensated by lower equity stake in production, implying \( d > d_a \). The additional risks of losing their investment in the bad aggregate state makes marginal utility of households in that state even higher. This prompts households to make more deposits at the bank for precautionary purposes. Finally, the loan size increases because banks make more profit from both equity holding (\( \bar{\theta} g(k) - d_a \)) and trading shares (\( (1 - \sigma_h)qN \)), which lure more competitive banks to enter the commercial banking industry. The end result is that the size of the commercial banking activity in the form of loans and deposits expands under asymmetric information. On the other hand, this spurt in commercial banking activity also leads to an increased volatility of household’s consumption.

Since households bear greater consumption risk in the asymmetric information environment, it entails welfare loss compared to the full information baseline scenario. In the following proposition, we establish that for a range of interest rates, the expected utility under asymmetric information (\( EU_a \)) is less than the baseline full formation expected utility (\( EU \)).
Proposition 4: $EU > EU_a$

Proof: Appendix E.

A few comments are in order before concluding this section. When banks sell stocks upon news, there is a redistributive element where banks receive $(1 - \sigma_h)C$ from households (in equilibrium, $qN = z = C$). The inefficiency is thus rooted in two elements: $q$ is traded at a discount (proposition 2) and an increase in precautionary savings ($s$) (proposition 3). Both lead to a loss of welfare manifested in greater consumption risk (proposition 2). Here, a tax on trading could partially ameliorate this welfare loss.\(^\text{22}\)

A. Endogenous Interest Rate

The analytical results in propositions 2 and 3 are established in the neighborhood of a full information equilibrium and also with an assumption of a small open economy which means that the real interest rate is exogenous. In this section, we perform a simulation experiment to check the robustness of these results. Assume logarithmic utility functions which mean $u(c_1) = \ln c_1$ and $v(c_2) = \ln c_2$. The production function is assumed to be Cobb-Douglas, meaning $g(k) = k^\alpha$ with $0 < \alpha < 1$. The interest rate ($r$) is now determined by the loan market equilibrium condition, $s = f$. There are nine parameters in this stylized model, namely $y, \sigma_h, \gamma, p, \alpha, \theta_g, \theta_b, C$ and $m$. The first period output $y$ is normalized at unity with a view to express relevant macroeconomic aggregates as a fraction of the first period output (GDP). The average growth rate of the economy is then $\sigma_h \tilde{\theta} k^\alpha + (1 - \sigma_h)m\^{\text{23}}$ After fixing the capital share parameter $\alpha$ at its conventional value 0.36, the remaining parameters are fixed to target a near zero average quarterly growth rate of GDP in the US and a real interest rate of 4.62% (computed by subtracting the bank prime rate from the CPI rate of inflation)\(^\text{24}\) during the crisis period 2004Q1-2008Q4.\(^\text{25}\) Table 1 summarizes the baseline parameter values.

Table 2 compares two economies: (i) with symmetric information (Symm Info), (ii) with asymmetric information (Asymm Info) for different probabilities of low signal states $(1 - \sigma_h)$.

\(^{\text{22}}\)One has to take into account that such a tax also penalizes the honest banks who sell due to adverse liquidity. An optimal tax can be designed which is beyond the scope of this paper.

\(^{\text{23}}\)In the context of our two period steady state model, the ratio of the second period to first period outputs approximates the long run average GDP growth rate.

\(^{\text{24}}\)The Federal Reserve Bank of St Louis database is used to arrive at these summary measures for output growth and real interest rate.

\(^{\text{25}}\)Given the stylized nature of this two period model, we do not aim to fully calibrate our model economy. The goal of this simulation is rather to illustrate the comparative statics effects on relevant aggregates setting parameters at reasonable values. These comparative statics results are robust to alternative choice of parameter values.
Table 1: Baseline Parameters

<table>
<thead>
<tr>
<th>$\alpha$</th>
<th>$y$</th>
<th>$b$</th>
<th>$g$</th>
<th>$h$</th>
<th>$\theta_q$</th>
<th>$\sigma_h$</th>
<th>$\gamma$</th>
<th>$p$</th>
<th>$m$</th>
<th>$C$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.36</td>
<td>1.00</td>
<td>1.00</td>
<td>2.25</td>
<td>0.92</td>
<td>0.766</td>
<td>0.6</td>
<td>0.05</td>
<td>0.1</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

The appendix describes the key equation system and the methodology for this model simulation. The lemon effect on the stock market is reflected by a sharply lower stock price ($q$) in the economy with information friction and a higher consumption volatility ($c$-vol) measured by the standard deviation of consumption levels for two dates and states together. In conformity with proposition 3, when information friction is present, banks hold a higher equity stake (thus lower $d/y$) in the borrowing firms and issue more loans (higher $f/y$). While the households also save more as a precautionary motive, the loan demand far outpaces the supply ($f > s$) which explains why the real interest rate rises. A higher interest rate raises the opportunity cost of investment (see eqns v and va in propositions 1 and 2) and has an adverse output effect. Consumption volatility is higher when information friction is present. Notice also that a greater probability of a low aggregate state (higher $1 - \sigma_h$) simply magnifies all these effects. All these results are in conformity with propositions 2 and 3.

Table 2: Effect of a change in the probability of low signal state

<table>
<thead>
<tr>
<th>$\sigma_h$</th>
<th>$q$</th>
<th>$d/y$</th>
<th>$f/y$</th>
<th>$r(%)$</th>
<th>output effect</th>
<th>$c$ volatility</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.92</td>
<td>Symm Info</td>
<td>0.27</td>
<td>0.79</td>
<td>0.20</td>
<td>4.56%</td>
<td>$-0.27%$</td>
</tr>
<tr>
<td></td>
<td>Asymm Info</td>
<td>0.13</td>
<td>0.64</td>
<td>0.30</td>
<td>5.12%</td>
<td>0.46</td>
</tr>
<tr>
<td>0.91</td>
<td>Symm Info</td>
<td>0.30</td>
<td>0.76</td>
<td>0.22</td>
<td>3.4%</td>
<td>$-0.31%$</td>
</tr>
<tr>
<td></td>
<td>Asymm Info</td>
<td>0.13</td>
<td>0.62</td>
<td>0.32</td>
<td>4.04%</td>
<td>0.45</td>
</tr>
<tr>
<td>0.90</td>
<td>Symm Info</td>
<td>0.34</td>
<td>0.74</td>
<td>0.24</td>
<td>2.22%</td>
<td>$-0.35%$</td>
</tr>
<tr>
<td></td>
<td>Asymm Info</td>
<td>0.12</td>
<td>0.59</td>
<td>0.34</td>
<td>2.93%</td>
<td>0.44</td>
</tr>
</tbody>
</table>

In Table 3, we perform similar sensitivity analysis by varying the probability $(1 - \gamma)$ of the liquidity crisis state. The effect of information friction is again the same as in propositions 2 and 3. A greater probability of a liquidity crisis (lower $\gamma$) heightens the speculative motive of households for saving which lowers the interest rate in both economies with or without information friction. Banks keep a lower equity stake and also push less loans in response to a greater anticipation of a liquidity crisis because of the looming insolvency. The output effects

---

26 Note that bank’s equity share is simply $\{1 - (d/y)\}*100\%$.
27 The adverse output effect of information friction, however, depends on the risk aversion parameter. We have specialized to a log utility function which means the relative risk aversion parameter is unity. For a more general power utility function, a higher relative risk aversion parameter entails greater precautionary savings which could reverse the direction of the output effect because the supply of loans could then outpace the demand.
of information friction is insensitive to change in $\gamma$ and so is the consumption volatility. 

Table 3: Effect of a change in the probability of liquidity crisis

<table>
<thead>
<tr>
<th>$gamma$</th>
<th>$q$</th>
<th>$d/y$</th>
<th>$f/y$</th>
<th>$r$ (%)</th>
<th>output effect</th>
<th>$c$ volatility</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.766</td>
<td>Symm Info</td>
<td>0.27</td>
<td>0.79</td>
<td>0.20</td>
<td>4.56%</td>
<td>-0.27%</td>
</tr>
<tr>
<td></td>
<td>Asymm Info</td>
<td>0.13</td>
<td>0.64</td>
<td>0.30</td>
<td>5.12%</td>
<td>0.46</td>
</tr>
<tr>
<td>0.75</td>
<td>Symm Info</td>
<td>0.27</td>
<td>0.80</td>
<td>0.19</td>
<td>2.22%</td>
<td>-0.28%</td>
</tr>
<tr>
<td></td>
<td>Asymm Info</td>
<td>0.13</td>
<td>0.66</td>
<td>0.29</td>
<td>2.76%</td>
<td>0.47</td>
</tr>
<tr>
<td>0.74</td>
<td>Symm Info</td>
<td>0.27</td>
<td>0.81</td>
<td>0.18</td>
<td>0.72%</td>
<td>-0.28%</td>
</tr>
<tr>
<td></td>
<td>Asymm Info</td>
<td>0.13</td>
<td>0.67</td>
<td>0.28</td>
<td>0.12%</td>
<td>0.47</td>
</tr>
</tbody>
</table>

Table 4 reports the sensitivity analysis of a change in the size of the liquidity shock, $C$. While the size of the liquidity shock has near zero consequence for symmetric information economy, it has significant effects on the economy with information frictions. This difference in effects arises particularly due to the fact that $C$ appears in the bank’s equilibrium profit equation (see equation 10). Banks issue lemon shares with a pretense of a liquidity crunch and in equilibrium banks can issue shares worth the size of the liquidity shock, $C$. Thus a greater size of the liquidity shock provides an incentive to the banks to hold a greater equity stake in borrowing firms (lower $d/y$) and push more loans ($f/y$) because banks make more profit by selling lemon shares. The equilibrium interest rate in economies with asymmetric information is higher which reflects bank’s propensity to create more loan demand that far outpaces the household savings. A higher interest rate has an adverse output effect because investment responds negatively to interest rate via proposition 2v(a). Consumption volatility in economies with information friction is significantly higher when the size of the liquidity shock is higher. This happens because in the presence of information friction, household’s equilibrium consumption in the low signal state ($c_{2l}$) is $s - C$ which responds negative to a rise in $C$.

Table 4: Effect of a change in the size of the liquidity shock

<table>
<thead>
<tr>
<th>$C$</th>
<th>$q$</th>
<th>$d/y$</th>
<th>$f/y$</th>
<th>$r$ (%)</th>
<th>output effect (%)</th>
<th>$c$ volatility</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.1</td>
<td>Symm Info</td>
<td>0.27</td>
<td>0.79</td>
<td>0.20</td>
<td>4.56%</td>
<td>-0.27%</td>
</tr>
<tr>
<td></td>
<td>Asymm Info</td>
<td>0.13</td>
<td>0.64</td>
<td>0.30</td>
<td>5.12%</td>
<td>0.46</td>
</tr>
<tr>
<td>0.15</td>
<td>Symm Info</td>
<td>0.28</td>
<td>0.79</td>
<td>0.20</td>
<td>4.56%</td>
<td>-0.41%</td>
</tr>
<tr>
<td></td>
<td>Asymm Info</td>
<td>0.14</td>
<td>0.57</td>
<td>0.35</td>
<td>5.4%</td>
<td>0.53</td>
</tr>
<tr>
<td>0.2</td>
<td>Symm Info</td>
<td>0.28</td>
<td>0.81</td>
<td>0.20</td>
<td>4.56%</td>
<td>-0.54%</td>
</tr>
<tr>
<td></td>
<td>Asymm Info</td>
<td>0.14</td>
<td>0.50</td>
<td>0.40</td>
<td>5.68%</td>
<td>0.60</td>
</tr>
</tbody>
</table>

---

$^{28}$The effect of a change in $p$ is not reported here for brevity. Such a change in project risk has very little effects on the economy except the loan size and contingent payments. In response to a higher project downside risk (lower $p$), banks cut back loans ($f$) and contingent payments ($d$) to the borrowers significantly.

20
B. What drives the stock market discount?

The upshot of this paper is that the information friction due to bank’s conflict of interest could give rise to a lemon problem which could translate into a stock market discount. The model predicts that such a discount (measured by the percent change in \( q \) from the symmetric information scenario) could be quite deep. For example, at the baseline parameter values, the stock market discount is about 52%. The size of the discount is crucially determined by the relative proportion of lemon in the stock market. Recall that the relative proportion of lemon is \((1-\sigma_h)/(1-\gamma)\sigma_h\) which is decreasing in \(\sigma_h\) and increasing in \(\gamma\). Thus a higher probability of a low aggregate state (lower \(\sigma_h\)) and/or a lower probability of liquidity crisis (higher \(\gamma\)) heightens this stock market discount. This results in a higher consumption volatility because investors demand a larger risk premium on shares. This basically summarizes the rational market’s reaction to the potential lemon problem.

V. Policy Experiments

A. Punishment

Suppose the government enforces a punishment in the form of a fine \(\Phi\) if banks misbehave. Let the probability of being caught for such a misbehavior be \(\lambda\). The expected profit of the bank then changes to:

\[
\pi_a^{bank} = \sigma_h \gamma \left[p\{\theta_g g(k) - d_g\} + (1 - p)\{\theta_b g(k) - d_b\}\right] \\
+ \sigma_h (1 - \gamma)(qN - C) + (1 - \sigma_h)[(1 - \lambda)(qN + m) - \lambda \Phi]) \\
- f(1 + r\sigma_h)
\]

Table 3 reports the effects of an increase in the fine amount setting the probability of detection \((\lambda)\) at 0.5. An increase in the size of the penalty has little effect on share prices and bank’s capital structure \(d/f\). However, the interest rate falls sharply due to such policy intervention. This happens because for a given interest rate, a higher penalty lowers the loan size at which the zero profit condition holds. \(^{29}\). Since the fine amount \(\Phi\) does not directly appear in the first order conditions of the household, it has little effect on savings at a given interest rate. The

\(^{29}\)To see this note that in the presence of fine \(f_a = \frac{\sigma_h \gamma (\theta g(k) - d_a) + (1 - \sigma_h) [(qN + m) - (1 - \lambda) \Phi]}{1 + r \sigma_h}\) which is lower than \(f_a\) as shown in proposition 2 for a given \(r\).
interest rate, therefore, adjusts downward to equilibrate in response to such a decline in loan demand. This raises investment and output. This effect is magnified if the fine amount is larger. The stock market discount due to information friction is also considerably less (39% for a hefty fine of \( \Phi = 2 \) as opposed to 52% when \( \Phi = 0 \)). Consumption volatility is also lower when the fine amount is larger. For a sufficiently large fine amount (around \( \Phi = 3 \)), it is possible to replicate the same consumption volatility as in a symmetric information economy.

<table>
<thead>
<tr>
<th>( \Phi )</th>
<th>Symm Info</th>
<th>Asymm Info</th>
<th>( q )</th>
<th>( d/y )</th>
<th>( f/y )</th>
<th>( r (%) )</th>
<th>output effect(%)</th>
<th>( c ) volatility</th>
<th>EU</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.0</td>
<td>0.27</td>
<td>0.79</td>
<td>0.20</td>
<td>4.56%</td>
<td>-0.27%</td>
<td>0.41</td>
<td>0.46</td>
<td>-0.43</td>
<td></td>
</tr>
<tr>
<td>0.5</td>
<td>0.27</td>
<td>0.79</td>
<td>0.20</td>
<td>4.56%</td>
<td>0.62%</td>
<td>0.40</td>
<td>0.45</td>
<td>-0.43</td>
<td></td>
</tr>
<tr>
<td>1.0</td>
<td>0.27</td>
<td>0.79</td>
<td>0.20</td>
<td>4.56%</td>
<td>1.32%</td>
<td>0.40</td>
<td>0.44</td>
<td>-0.43</td>
<td></td>
</tr>
<tr>
<td>2.0</td>
<td>0.27</td>
<td>0.79</td>
<td>0.20</td>
<td>4.56%</td>
<td>2.75%</td>
<td>0.40</td>
<td>0.42</td>
<td>-0.43</td>
<td></td>
</tr>
</tbody>
</table>

Since the policy authority does not know precisely the node at which the bank operates at date 1.5, it is vulnerable to the same information friction as private citizens. The expected fine amount thus appears as a tax on all banks’ expected profit regardless of their deviant behaviour. As a result, the punishment is not costless to the society because it is a deadweight loss. This decreases welfare of private citizens which appears in the last column of Table 5.

**B. Ring fencing**

Will private citizens be better off if retails banks are "ring fenced" and legally mandated not to underwrite securities? The question is relevant in the present context of banking commission’s legislation. Using our model, we now demonstrate that in such a restricted environment when banks cannot diversify away the liquidity shocks by trading securities, full consumption risk sharing fails even under full information.

Consider an environment where retail banks and investment banks are separated. Retail banks only perform loan and depository activities while households mimic the operation of investment bankers by issuing securities to each other. Banks issue loans (\( F \)) to the household/entrepreneur and incur the same loan servicing cost as before. As in the previous scenario, there is a state of a global liquidity shock where all banks suffer a liquidity shock \( C \). However, unlike the universal banking regime, banks instead of issuing securities in a secondary share
market, call off the loan and sell the capital at a salvage value $m$. Thus we merge the two states $x$ and $l$ in a single state where in both states banks liquidate the project early and pay zero interest on saving deposits.

Bank’s zero expected profit condition thus changes to:

$$E \pi = \gamma \sigma_h (p R_g + (1 - p) R_b) - (1 - \gamma \sigma_h) m - \sigma_h (1 - \gamma) C - F (1 + r \sigma_h) \geq 0$$  \hspace{1cm} (12)$$

where $R_g$ and $R_b$ are the payments stipulated by the banks in good and bad states, $g$ and $b$. The expected profit of the bank reflects the following facts. First, the bank receives pay-off from the project only in the high state with no liquidity shock which explains the first term. Second, banks sell off the capital at the salvage value $m$ and do not pay interest in states $l$ and $x$, which explains the second term. Third, the liquidity shock $C$ hits the bank with the probability $\sigma_h (1 - \gamma)$ that explains the third term. Finally, the last term captures the fact that banks pay interest with probability $\sigma_h$.

For the household, we assume that a stand-in household holds a fractional claim $(x)$ to the value of the stock $(Q)$ at date 1 and issues out $(1 - x) Q$ to others. In equilibrium only a single share is traded (which means $x = 1$). The rest of the institutional arrangement is the same as in the earlier banking scenario.

Household’s flow budget constraints are now:

$$c_1 + s + k + x Q = y + Q + F$$  \hspace{1cm} (13)

$$c^{x}_{2g} = s (1 + r) + x f(k) \theta^h - R_g$$  \hspace{1cm} (14)

$$c^{x}_{2b} = s (1 + r) + x f(k) \theta^l - R_b$$  \hspace{1cm} (15)

$$c^x_2 = c_l = s$$  \hspace{1cm} (16)

The optimal control problem is:

$$\text{Max} \quad u(c_1) + \sigma_h \gamma [p v(c^{x}_{2g}) + (1 - p) v(c^{x}_{2b}) + \sigma_h (1 - \gamma) v(c^x_2) + (1 - \sigma_h) v(c_l)$$  \hspace{1cm} (17)$$

subject to the flow budget constraints (13) through (16) and the zero profit condition (12).
It is straightforward to check now that derivative of the maximand (17) with respect to the debt instruments $R_g$ and $R_b$ yields the following risk sharing condition. The Appendix G provides details of the derivation.

$$\frac{u'(c_1)}{1 + r \sigma_h} = v'(c_{2g}^{ns}) = v(c_{2b}^{ns})$$

(18)

which means that $c_{2g}^{ns} = c_{2b}^{ns}$. Thus debt instruments can eliminate the idiosyncratic risks in a state of no liquidity shock.\(^{30}\) However, full consumption insurance is not possible because $c_{2g}^{ns} = c_{2b}^{ns} \neq c_2 = c_l$. In addition, a positive risk premium $(RP)$ arises that is given by the following expression:

$$RP = \frac{(1 - \gamma \sigma_h)u'(s)}{\gamma \sigma_h} > 0$$

(19)

The failure of full consumption risk sharing and the emergence of a positive risk premium stands in sharp contrast with universal banking. In the latter case, the presence a secondary stock market mimics a complete market scenario and enables the household to strike full consumption insurance through the efficient operation of the equity market. On the other hand, in a stand alone banking system, the financial markets are fundamentally incomplete due to insufficient number of financial instruments. This makes full consumption insurance impossible.\(^{31}\)

The issue still arises whether private citizens could be better off in a stand alone banking system as opposed to a universal banking environment where information friction is endemic. Table 6 makes an expected utility comparison of the stand alone banking system with the universal banking system with information friction around the baseline values of the probabilities, $\sigma_h$ and $\gamma$. The same log utility and Cobb-Douglas production functions specifications are used for this comparison. The expected utility is uniformly higher in the latter banking arrangement. One needs to be careful about this kind of expected utility comparison because such a comparison is very model specific and it does not capture numerous features of both banking systems. Nevertheless, one can at best conclude that everything else equal, private welfare is higher in a scenario of universal banking where risk diversification opportunities exist even though conflict of interest between bankers and share holders is pervasive as opposed to a stand alone banking regime where all these risk sharing opportunities are shut down by legal mandate.

\(^{30}\)Note that unlike universal banking optimal $R_g$ is not equal to $R_b$. Rather $R_g - R_b = (\theta^s - \theta^b)f(k)$ to ensure consumption equalization between good and bad states.

\(^{31}\)In a companion paper with borrower’s moral hazard (Banerjee and Basu, 2010), we arrive at similar conclusion.
Table 6: Expected utilities in universal and stand alone banking systems

<table>
<thead>
<tr>
<th>$\gamma$</th>
<th>$\sigma_h$</th>
<th>0.766</th>
<th>0.78</th>
<th>0.79</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.92</td>
<td>$EU^u = 0.42$</td>
<td>$EU^u = 0.42$</td>
<td>$EU^u = 0.41$</td>
<td></td>
</tr>
<tr>
<td></td>
<td>$EU^n = 0.97$</td>
<td>$EU^n = 0.95$</td>
<td>$EU^n = 0.93$</td>
<td></td>
</tr>
<tr>
<td>0.93</td>
<td>$EU^u = -0.40$</td>
<td>$EU^u = -0.40$</td>
<td>$EU^u = -0.39$</td>
<td></td>
</tr>
<tr>
<td></td>
<td>$EU^n = -0.97$</td>
<td>$EU^n = -0.93$</td>
<td>$EU^n = -0.91$</td>
<td></td>
</tr>
<tr>
<td>0.94</td>
<td>$EU^u = -0.38$</td>
<td>$EU^u = -0.38$</td>
<td>$EU^u = -0.38$</td>
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</tr>
<tr>
<td></td>
<td>$EU^n = -0.95$</td>
<td>$EU^n = -0.92$</td>
<td>$EU^n = -0.89$</td>
<td></td>
</tr>
</tbody>
</table>

Note: $EU^u =$ Expected utility in the universal banking and $EU^n =$ Expected utility in the stand alone banking.

VI. Conclusion

The universal banking system has been a subject of controversy, especially in the wake of current financial crisis. The critics argue that such a system could inflict excessive risks on the financial system. In this paper, we evaluate the nature of such risks and the consequent impact on overall banking activities. We find that discounting of stocks, volatilities in consumption, pushing of loans and excessive savings could emerge if hidden information is pervasive and if particularly the probability of bad aggregate shock is high.

The major policy question still remains open whether this information friction is severe enough to warrant ring fencing of the retail banking system or punishing all banks in terms of a punitive tax which could restrict financial intermediation. Our model based analysis suggests that such an across the board punitive tax on all bankers regardless of their deviant status could pose a deadweight loss on the society. On the other hand, ring fencing retail banking as per the independent banking commission’s recommendation could depress national welfare even further because of the legal restriction on devitrification. In other words, financial inefficiency generated by ring fencing could far outweigh the benefits of eliminating information friction. The universal banking could work well and produce the optimal outcome if the regulatory authorities are committed to enforce strict disclosure of regimes to eliminate the information frictions.

Appendix

A. Equilibrium Conditions

In equilibrium, three conditions hold:

1. Each bank stipulates an optimal contract laid out in proposition 1 with each household
taking the average capital stock, $K$ and average contingent payments $d$ as given.

2. Expectations are consistent which means $k = K$.

3. All markets clear which means:

- In the contingent claims market at date 1, each bank’s state contingent shares are given by $\frac{\theta_g(k) - d_g}{\theta_g(k)}$ and $\frac{\theta_b(k) - d_b}{\theta_b(k)}$, while household’s shares are given by $\frac{d_g}{\theta_g(k)}$ and $\frac{d_b}{\theta_b(k)}$.

- In the secondary share market at date 1.5, the demand for shares equals the supply which means $qN = z = C$.

- Goods markets clear at each date which mean
  - At date 1, $c_1 + k = y + NFI$
  - At date 2,

$$\sigma_h[p\theta_g + (1 - p)\theta_b]g(k) + (1 - \sigma_h)m - \sigma_h(1 - \gamma)C(1 + r) - NFI(1 + r\sigma_h) = Ec_2 \equiv$$

$$\sigma_h[pc_{2g}^* + (1 - p)c_{2b}^*] + \sigma_h(1 - \gamma)[pc_{2g} + (1 - p)c_{2b}] + (1 - \sigma_h)c_2$$

(20)

The following remarks about market clearing conditions are in order: First the contingent claims $d_i$ are not traded in a market. These are stipulated by optimal contracts and that is why there is no price attached to each such contingent claim. Second, the secondary shares are traded in a market that opens at date 1.5. The demand for such shares is $z$ which is the amount a household agent apportions from her savings. The supply is the amount that banks issue consequent on a liquidity shock. We assume that given $q$, banks issue shares exactly worth the amount of the exogenous liquidity crunch $C$. This means that $qN = z = C$.

Third, about the date 1 goods market clearing conditions, one needs to note that since interest rate is exogenous, the imbalance between saving ($s$) and loan ($f$) has to be financed by net foreign investment ($NFI \equiv f - s$) which explains the presence of the term $NFI$. Finally, the date 2 goods market clearing condition basically means that the right hand side term which is the consumption plus the foreign debt retirement aggregated across all individuals must balance the corresponding left hand side term which is the aggregate output net of the liquidity shock.
including the interest payment on it. Since this shock is exogenous, it appears like a tax on date 2 output. This explains the presence of the term $\sigma_h(1 - \gamma)C(1 + r)$ on the left hand side of (20). \footnote{It is easy to verify that the Walras law holds here so that if all but one market clears, then adding all the budget constraints would ensure that the remainder market must clear as well. To see this, one can plug the budget constraints (4) through (9) and the zero profit condition ((vi) in Proposition 1 into the date 2 aggregate demand for good $(E_{c2})$ and by using the secondary market equilibrium condition $(q_s = C = Z)$ in the resulting expression will verify that the market for goods at date 2 automatically clears.}

B. Proof of Proposition 1

Plugging consumption of individual agents in each contingency outlined above in the expected utility function, we get:

$$Max \ EU = \left[ u(y + f - s - k) \right] + \sigma_h [pv\{d_g + s(1 + r)\} + (1 - p)v\{d_b + s(1 + r)\}]$$

$$+ \sigma_h (1 - \gamma)[pv\{d_g + (s - z)(1 + r) + \frac{z}{q}EX\} + (1 - p)v\{d_b + (s - z)(1 + r) + \frac{z}{q}EX\}]$$

$$+(1 - \sigma_h)v(s)$$

subject to:

$$\pi^b = \sigma_h [p\{\theta_g g(k) - d_g\} + (1 - p)\{\theta_b g(k) - d_b\}] + (1 - \sigma_h)m - f(1 + r\sigma_h) = 0$$

First order conditions with respect to $d_g, d_b, s, k$ and $z$ respectively are:

$$d_g : \frac{\gamma u'(c_1)}{1 + r\sigma_h} = \gamma v'\left(c_{2g}^{n_2}\right) + (1 - \gamma)v'\left(c_{2g}^n\right)$$

(A1)

$$d_b : \frac{\gamma u'(c_1)}{1 + r\sigma_h} = \gamma v'\left(c_{2b}^{n_2}\right) + (1 - \gamma)v'\left(c_{2b}^n\right)$$

(A2)

$$s : \frac{u'(c_1)}{1 + r\sigma_h} = \gamma\sigma_h [pv\left(c_{2g}^{n_2}\right) + (1 - p)v\left(c_{2b}^{n_2}\right)]$$

(A3)

$$+(1 - \gamma)\sigma_h [pv\left(c_{2g}^n\right) + (1 - p)v\left(c_{2b}^n\right)](1 + r) + (1 - \sigma_h)v'(c_2)$$

$$k : u'(c_1)[\sigma_h \gamma \bar{g}'(k) - (1 + r)] = 0$$

(A4)

$$z : \left[ pv'\left(c_{2g}^n\right) + (1 - p)v'\left(c_{2b}^n\right) \right] \left( \frac{EX}{q} - (1 + r) \right) \geq 0$$

(A5)
(i) We will show now that $d_g = d_b = d$.

Let us suppose that $d_g > d_b$. Let us make the adjustment such that $d_g$ is reduced and $d_b$ is increased so as to reduce the gap in such a way that the zero profit constraint is not affected, i.e. $[pd_g + (1 - p)d_b]$ is constant. Hence, $[p(d_g - \Delta_1) + (1 - p)(d_b + \Delta_2)]$ is a constant so that $(1 - p)\Delta_2 = p\Delta_1$.

Now, evaluate the expected utility with small increments that satisfy the above equality.

$$
\Delta EU = \sigma_h [\gamma \{ -pu'(c_{2g}^{nx})\Delta_1 + (1 - p)u'(c_{2b}^{nx})\Delta_2 \} + (1 - \gamma)\{ -pv'(c_{2g}^{nx})\Delta_1 + (1 - p)v'(c_{2b}^{nx})\Delta_2 \}]
$$

$$\Rightarrow \Delta EU = \sigma_h [\gamma \{ u'(c_{2g}^{nx}) - u'(c_{2b}^{nx}) \} + (1 - \gamma)\{ v'(c_{2g}^{nx}) - v'(c_{2b}^{nx}) \}][(1 - p)\Delta_2 > 0 \quad (A6)]$$

Since, $c_{2g}^{nx} < c_{2b}^{nx}$ it implies that $u'(c_{2g}^{nx}) - u'(c_{2b}^{nx}) > 0$ (due to concave utility function) and since $c_{2b}^{nx} < c_{2g}^{nx}, v'(c_{2g}^{nx}) - v'(c_{2b}^{nx}) > 0$ and $\Delta_2 > 0$ because $d_b$ was increased.

Hence, adjustment can be made until $u'(c_{2g}^{nx}) - v'(c_{2b}^{nx}) = 0$ and $v'(c_{2b}^{nx}) - v'(c_{2g}^{nx}) = 0$. Hence, $c_{2b}^{nx} = c_{2g}^{nx}$ and $c_{2g}^{nx} = c_{2b}^{nx}$ which implies $d_g = d_b$.

One can start with the reverse inequality $d_g < d_b$ and make the opposite adjustments to reach this equality. This proves (i).

(ii) and (iii): From (A5), it follows that $(E\tilde{X}/q - (1 + r)) = 0$ and plugging the result in $c_{2g}^{z} = d_g + (s - z)(1 + r) + \frac{\gamma}{q}E\tilde{X}$ and $c_{2b}^{z} = d_b + (s - z)(1 + r) + \frac{\gamma}{q}E\tilde{X}$ and using the result from (i) that $d_g = d_b = d$ yields $c_{2g}^{nx} = c_{2b}^{nx} = c_{2g}^{z} = c_{2b}^{z} = c_2$ (say). This proves (ii) and (iii).

(iv) The equation (A3) can be written as

$$
\frac{u'(c_1)}{1 + r\sigma_h} = \sigma_h [\gamma u'(c_{2g}^{nx}) + (1 - \gamma)u'(c_{2b}^{nx}) + (1 - p)(\gamma u'(c_{2b}^{nx}) + (1 - \gamma)u'(c_{2g}^{nx}))](1 + r) + (1 - \sigma_h)u'(c_{2l})
$$

Plugging (A1) and (A2), $\frac{u'(c_1)}{1 + r\sigma_h} = \sigma_h \frac{u'(c_1)(1 + r)}{1 + r\sigma_h} + (1 - \sigma_h)u'(c_{2l})$ and by rearrangement, we get:

$$
u'(c_1) = \left[ \frac{(1 - \sigma_h)(1 + r\sigma_h)}{1 - \gamma\sigma_h + (1 - \gamma)\sigma_h} \right] u'(s)
$$

which proves (iv).

The part (v) follows from the straightforward differentiation with respect to $k$ and the binding zero profit constraint of the intermediary together with (i) yields the last proposition. //
C. Proof of Proposition 2

Using the same line of reasoning as in Proposition 1, one can establish that

\[ v'(c_{2b}^{\frac{n}{x}}) - v'(c_{2g}^{\frac{n}{x}}) = 0 \]  

(B1)

and

\[ v'(c_{2b}^{g}) - v'(c_{2g}^{g}) = 0 \]  

(B2)

On the other hand, the first order condition for \( z \) is:

\[ v'(d_a + (s_a - z)(1 + r) + \frac{z}{q_a} \tilde{E}X_a) \cdot \left\{ \frac{E\tilde{X}}{q_a} - (1 + r) \right\} \sigma_h(1 - r) = v'(s_a - z)(1 - \sigma_h) \]

Since \( v'(\cdot) > 0 \Rightarrow \frac{E\tilde{X}}{q_a} - (1 + r) > 0 \Rightarrow c_{2g}^{g} > c_{2b}^{g} \). Hence, (B1) and (B2) can hold if

\[ c_{2g}^{g} = c_{2b}^{g} > c_{2g}^{x} = c_{2b}^{x} \]  

(B3)

The part (ia) follows from the above result and the two first order conditions with respect to \( \{d_a, d_b\} \)

\[ d_a : \frac{\gamma v'(c_{1})}{1 + \gamma \sigma_h} = \gamma v'(c_{2b}^{x}) + (1 - \gamma)v'(c_{2g}^{x}) \]

\[ d_b : \frac{\gamma v'(c_{1})}{1 + \gamma \sigma_h} = \gamma v'(c_{2b}^{g}) + (1 - \gamma)v'(c_{2g}^{g}) \]

The part (iia) follows directly from the first order with respect for \( z \), which is,

\[ v'(d_a + (s_a - z)(1 + r) + \frac{z}{q_a} \tilde{E}X_a) \left\{ \frac{E\tilde{X}}{q_a} - (1 + r) \right\} \{\sigma_h(1 - \gamma)\} = v'((s_a - z)(1 - \sigma_h) \}

The part (iiia) follows from (B3) and (ia).

Finally, (iva) and (va) can be shown exactly using similar line of reasoning as in the earlier section. //

D. Proof of Proposition 3

All variables are evaluated at their full information values obtained in the proposition 1. This means that we start from a full information equilibrium with zero information friction. Thus at date 1, in the absence of information friction, \( c_1 = c_{1a} \). Given the same \( r \), it means that \( k = k_a \).

From the date 1 resource constraint (4), it follows that \( f - s = f_a - s_a \).
Starting from this scenario of no information friction, with the onset of information friction, $z$ and the risk premium terms turn positive from 0. Given $c_1 = c_{1a}$, from proposition 1(iv) and proposition 2(iv) it follows that $v'(s) = v'(s_a - z)$ which means that $s < s_a$. Since $f - s = f_a - s_a$, the immediate implication is that $f < f_a$.

Next compare the expressions for $f$ and $f_a$ in proposition 1(vi) and proposition 2vi(a) evaluated at equilibrium $qN = C$ and note that since $f - f_a < 0$, the following inequality holds

$$\gamma \sigma_h (d - d_a) + C (1 - \sigma_h) > 0$$

For a sufficiently small $C$, the above inequality means that $d > d_a$ //

E. Proof of Proposition 4

Using the risk sharing results from proposition 2, the expected utility ($EU_a$) in (10) can be written in a compact form as:

$$EU_a = u(y + f_a - s_a - k) + \sigma_h [\gamma v(c_{2a}^{nx}) + (1 - \gamma) v(c_{2a}^x)] + (1 - \sigma_h) v(c_{2a})$$

Next note that the expected utility under full information (with full risk sharing) is given by:

$$EU = u(y + f - s - k) + \sigma_h v(c_2) + (1 - \sigma_h) v(c_2^x)$$

Since our baseline of comparison is full information equilibrium, by construction $f - s = f_a - s_a$ and $c_2^x = c_{2a}^x$ (see proposition 3).

The comparison of two expected utilities $EU$ and $EU_a$ thus hinges on the relative magnitudes of $v(c_2)$ and $[\gamma v(c_{2a}^{nx}) + (1 - \gamma) v(c_{2a}^x)]$. Note from proposition 1(iii) that $c_2 = s(1 + r) + d$. On the other hand, recall from proposition 2(iii), $c_{2a}^{nx} = d_a + s_a(1 + r)$ and $c_{2a}^x = d_a + s_a(1 + r) + \left\{ \frac{E\tilde{X}_a}{q} - (1 + r) \right\} \cdot c$.

Since the comparison is made in the neighbourhood of a full information equilibrium, we set the interest rate $r$ such that

$$c_2 = \gamma c_{2a}^{nx} + (1 - \gamma) c_{2a}^x$$
By strict concavity of the utility function (applying Jensen’s inequality), it then follows that \( v(c_2) > \gamma v(c^2_{2a}) + (1 - \gamma)v(c^2_{2a}) \). This proves that \( EU > EU_a \). //

F. Methodology for Model Simulation

Case of symmetric Information

With a log utility function and Cobb-Douglas production function \( g(k) = k^\alpha \) the equation system in Proposition 1 reduces to:

\[
\gamma(d + s(1 + r)) = (1 + r \sigma_h)c_1 \quad \text{based on (i)} \tag{21}
\]

\[
s = \left[ \frac{(1 - \sigma_h)(1 + r \sigma_h)}{1 - \gamma \sigma_h + r \sigma_h(1 - \gamma)} \right] c_1 \quad \text{based on (iv)} \tag{22}
\]

\[
k = \left[ \frac{1 + r \sigma_h}{\gamma \sigma_h \theta \alpha} \right] \frac{1}{1 - \sigma_h} \quad \text{based on (v)} \tag{23}
\]

\[
f = \sigma_h \gamma(\theta k^\alpha - d) + \frac{(1 - \sigma_h)m}{1 + r \sigma_h} \quad \text{based on (vi) after plugging } qN - C = 0 \tag{24}
\]

Given the loan market clearing condition \( s = f \), the first period resource constraint for the economy reduces to \( c_1 + k = y \) which after plugging into (22) and (23), one gets

\[
\gamma(d + s(1 + r)) = (1 + r \sigma_h)(y - k) \quad \text{based on (vii) after plugging } qN - C = 0 \tag{25}
\]

\[
s = \left[ \frac{(1 - \sigma_h)(1 + r \sigma_h)}{1 - \gamma \sigma_h + r \sigma_h(1 - \gamma)} \right] (y - k) \quad \text{based on (vii) after plugging } qN - C = 0 \tag{26}
\]

Eqs (23), (24), (25) and (26) solve for \( d, f, k, r \). The security price \( q \) can be obtained by using the equation \( q = \frac{\theta k^\alpha - d}{1 + r} \).

Case of Asymmetric Information

With the same log utility function and the Cobb-Douglas production function, the risk sharing condition (ia) in Proposition 2 (together with the loan market clearing condition, \( s_a = f_a \))
and the share market clearing condition \( z = C \) reduces to

\[
\frac{\gamma}{(y - k_a)(1 + r_a \sigma_h)} = \frac{\gamma}{d_a + s_a(1 + r_a)} + \frac{1 - \gamma}{d_a + s_a(1 + r_a) + RP \cdot C}
\]  

(27)

where \( RP \) stands for risk premium equal to \( \left\{ \hat{E}\hat{X}_{a} - (1 + r_a) \right\} \) and the subscript \( a \) stands for the interest in the asymmetric information scenario.

Next use the expression for risk premium in Proposition 2(iia) and solve the equilibrium \( RP \) (imposing the aggregate consistency condition \( k = K \)) explicitly as follows:

\[
RP = \lambda_1 \cdot \frac{(d_a + f_a(1 + r))}{f_a - C(1 + \lambda_1)}
\]

(28)

where

\[
\lambda_1 = \frac{1 - \sigma}{\sigma(1 - \gamma)}
\]

After plugging the goods market clearing condition \( c_1 + k = y \) and the loan market and share market clearing conditions \( f_a = s_a \) and \( z = C \), Proposition 2(iv) reduces to

\[
(f_a - C) = \left[ \frac{(1 - \sigma_h)(1 + r_a \sigma_h)}{1 - \gamma \sigma_h + r_a \sigma_h(1 - \gamma)} \right] (y - k_a)
\]

(29)

The investment equation is the same as before and can be written as:

\[
k_a = \left[ \frac{1 + r_a \sigma_h}{\gamma \sigma_h \theta a} \right]^{\frac{1}{1 - \sigma}}
\]

(30)

Finally the zero profit condition reduces to

\[
f_a = \sigma_h \gamma \left( \hat{g}(k_a) - \hat{d}_a \right) + (1 - \sigma_h)(m + C)
\]

\[
\frac{1}{1 + r_a \sigma_h}
\]

(31)

Eq (27) through (31) can be solved for five unknowns, \( f_a, d_a, r_a, k_a, RP \). The resulting share price \( q_a \) is given by \( \frac{\sigma h \gamma - \hat{d}_a}{1 + r_a + RP} \).

G. Case of Stand-alone banking system

Let \( \lambda_1, \lambda_2, \lambda_3, \lambda_4 \) be the lagrange multipliers associated with (13),(14),(15) and (12) respectively.
By using (33), (34), (37) and (38), (36) and (32), one gets

\begin{align*}
\frac{\partial}{\partial c_{nx}} (c_{nx}^2 g) &= 0 = \lambda_1 + (1 + \gamma) = 0 \\
\frac{\partial}{\partial c_{nx}} (c_{nx}^2 b) &= 0 = \lambda_2 + (1 + \gamma) = 0 \\
\frac{\partial}{\partial c_{nx}} (c_{nx}^2) &= 0 = \lambda_3 + (1 + \gamma) = 0 \\
\frac{\partial}{\partial s} (s) &= 0 = \lambda_4 + (1 + \gamma) = 0 \\
\frac{\partial}{\partial F} (F) &= 0 = \lambda_5 + (1 + \gamma) = 0 \\
\frac{\partial}{\partial R_g} (R_g) &= 0 = \lambda_6 + (1 + \gamma) = 0 \\
\frac{\partial}{\partial R_b} (R_b) &= 0 = \lambda_7 + (1 + \gamma) = 0 \\
\frac{\partial}{\partial x} (x) &= 0 = \lambda_8 + (1 + \gamma) = 0 \\
\frac{\partial}{\partial k} (k) &= 0 = \lambda_9 + (1 + \gamma) = 0
\end{align*}

Using (33), (34), (37) and (38), (36) and (32), one gets

\begin{align*}
v'(c_{nx}^2 g) &= v'(c_{nx}^2 b) = v'(c_{nx}) = \frac{v'(c_1)}{1 + r} \\
&= > c_{nx}^2 g = c_{nx}^2 b = c_{nx}^2 (say)
\end{align*}

which proves the risk sharing condition (18).

After substituting out the Lagrange multipliers from (35), one gets the following Euler equation for saving:

\begin{equation}
u'(c_1) = \gamma \sigma_h v'(c_{nx}^2)(1 + r) + (1 - \gamma) = 0(43)\end{equation}

Substituting the Lagrange multipliers from (39), one gets the following Euler equation for stock holding:

\begin{equation}u'(c_1) = \gamma \sigma_h v'(c_2) \frac{\bar{\theta} f(k)}{Q} = 0(44)\end{equation}

where \(\bar{\theta} = p \theta + (1 - p) \theta^f\). Subtracting (44) from (43), one gets the following expression for the stock market premium

\begin{equation}\frac{\bar{\theta} f(k)}{Q} - (1 + r) = \frac{(1 - \gamma \sigma_h) v'(s)}{\gamma \sigma_h} = 0(45)\end{equation}
Substituting out the lagrange multipliers from (40), one gets the Euler equation with respect to $k$:

$$u'(c_1) = \sigma_h \gamma v'(c_2^{nx}) \theta f(k)$$ \hfill (46)

Using the the risk sharing condition (42) and the flow budget constraints, one gets the following equations for debt instruments;

$$R_g - R_b = (\theta^g - \theta^b)f(k)$$ \hfill (47)

Using (32), (36), (37), and (938) one gets the Euler equation with respect to $F$:

$$u'(c_1) = (1 + r\sigma_h)v'(c_2^{nx})$$ \hfill (48)

Thus equations 35), (48),(40), (12) and (47) together with the flow budget constraints (13) through (16) and the loan market clearing condition $F = s$, determine five endogenous variables $k, s, r, R_g$ and $R_b$ based on the following equations

$$u'(y - k) = \gamma \sigma_h v'(s(1 + r) + \theta^h f(k) - R_g)(1 + r) + (1 - \gamma \sigma_h)v'(s)$$ \hfill (49)

$$u'(y - k) = (1 + r\sigma_h)v'(s(1 + r) + \theta^h f(k) - R_g)$$ \hfill (50)

$$u'(y - k) = \sigma_h \gamma v'(s(1 + r) + \theta^h f(k) - R_g)\theta f'(k)$$ \hfill (51)

$$s = \frac{\gamma \sigma_h (pR_g + (1 - p)R_b) - (1 - \gamma \sigma_h)\theta^h(1 - \gamma)C}{1 + r\sigma_h}$$ \hfill (52)

$$R_g - R_b = (\theta^g - \theta^b)f(k)$$ \hfill (53)

References


